

# An approach to estimate carbon stocks change in forest carbon pools under the UNFCCC: the Italian case

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Under the UNFCCC, Annex I Parties must report annually a National GHG Inventories of anthropogenic emissions by sources and removals by sinks. LULUCF is one of the six sectors of the inventory: in this sector any emissions and removals of GHGs by land management should be reported, included the large GHGs fluxes generated by forest management and land-use changes into and from forest. In this context every Party has to produce a proper model in order to be able to fulfil GHGs Inventory request for forest sector. Taking Italy as a study case, the paper aims at presenting a new methodology for updating stock changes for years between national forest inventories, in order to reproduce annual stock changes in the five UNFCCC forest carbon pools, following the UNFCCC requirements in the context of carbon reporting.

**Keywords:** Carbon stock, GHG inventory, LULUCF, yield model, sink, C pools

## Introduction

Under the United Nations Framework Convention on Climate Change (UNFCCC) each industrialised country listed in Annex I of the Convention must report annually a National Greenhouse Gas Inventory of its anthropogenic emissions by sources and removals by sinks of greenhouse gases (GHGs) not controlled by the Montreal Protocol.

One out of six sectors of the inventory concerns Land Use, Land-Use Change and Forestry categories (LULUCF). In this sector any emissions and removals of GHGs by managed land should be reported. Among land uses, forest land use is one of the most relevant, due to large carbon pools and associated large GHGs fluxes generated by forest management and land-use changes into and from forest.

Interrelations between forest and climate system have been a major focus of research since mid-1980s. Up to date, several models have been developed that analyze and simu-

late carbon budgets and fluxes at level of forest stands. These tools range from very detailed models based on ecophysiological processes and driven by environmental parameters (*e.g.*, Waring & Running 1998) to very general empirical, descriptive models of carbon budgets within forest stands (*e.g.*, Masera et al. 2003). None of these models have been widely used for operational application, and none of them has been adopted as standard for carbon reporting under UNFCCC. As the main reason for this we consider the age dependency of all these models in which all stand variables being driven by the age of the forest/plantation. In reality, however, growth is strictly related to species and to local environmental conditions. In this respect the most realistic estimates of carbon stock changes have to be derived by yield models, whose input data are directly connected with National Forest Inventories (NFI). UNFCCC requirements in the context of carbon reporting also require a series of features for forest sector which are only compatible with yield models. Under current UNFCCC reporting guidelines (IPCC 2000, IPCC 2003) estimates of carbon stock changes in the forest sector must still be based on national forest inventories and yield models. In this context every Country is encouraged to produce a proper national model in order to be able to annually fulfil GHG's Inventory request for the forest sector.

To be utilized for UNFCCC reporting the model shall respond to some characteristics:

1. it shall be based on: (i) official statistical data like the National Forest Inventory and national forest statistics; (ii) peer reviewed scientific dataset;

2. it shall produce annual carbon stock changes in each carbon pool;
3. it shall be accurate and, in the Kyoto Protocol perspective, conservative (*i.e.*, neither overestimate increases nor underestimate decreases in carbon stocks in carbon pools).

A general complication for UNFCCC carbon reporting in the forestry sector is connected to the need of annual reporting since 1990, whereas NFI's are performed in cycles of 5-10 years in some countries with best case of NFI data availability. In Italy, for example, there is a NFI available for the year 1985 and a new NFI is still ongoing. Anyway, considering the timing of NFIs, there is the need of reporting carbon stock changes for any year between consecutive inventories with a reliable methodology, based on growth relationships and annually measured forest parameters, rather than a simple extrapolation between years.

Following the above rationale, we propose a new methodology, which is based on existing NFI data for 1985 and new forest area estimates from the ongoing NFI, in order to reproduce annual stock changes in the five UNFCCC forest carbon pools (IPCC 2003). Taking Italy as an example, the paper aims at presenting a methodology for updating stock changes for years between national forest inventories, which could eventually be used also for other countries with similar data availability (Tab. 1).

**Tab. 1** - Forest areas from 1985 to 2006.

Year	Forest area (kha)
1985	8675
1986	8793
1987	8908
1988	9028
1989	9145
1990	9263
1991	9380
1992	9498
1993	9616
1994	9733
1995	9851
1996	9968
1997	10086
1998	10203
1999	10321
2000	10438
2001	10556
2002	10674
2003	10791
2004	10909
2005	11026
2006	11144

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**Tab. 2** - Biomass Expansion Factors, Wood Basic Densities for aboveground biomass estimate and Root/Shoot ratio.

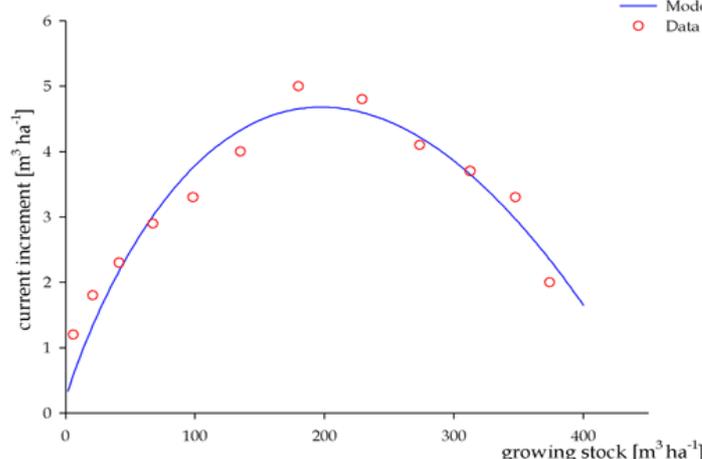
Typology	Inventory typology	BEF	Wood Basic Density	R	
		volume of above-ground biomass / volume of growing stock	Dry weight t/ fresh volume of above-ground biomass m <sup>3</sup>	weight of below-ground biomass / weight of growing stock	
Stands	norway spruce	1.29	0.38	0.29	
	silver fir	1.34	0.38	0.28	
	larches	1.22	0.56	0.29	
	mountain pines	1.33	0.47	0.36	
	mediterranean pines	1.53	0.53	0.33	
	other conifers	1.37	0.43	0.29	
	europaean beech	1.36	0.61	0.20	
	turkey oak	1.45	0.69	0.24	
	other oaks	1.42	0.67	0.20	
	other broadleaves	1.47	0.53	0.24	
	<i>partial total</i>	<i>1.35</i>	<i>0.51</i>	<i>0.28</i>	
Coppices	europaean beech	1.36	0.61	0.20	
	sweet chestnut	1.33	0.49	0.28	
	hornbeams	1.28	0.66	0.26	
	other oaks	1.39	0.65	0.20	
	turkey oak	1.23	0.69	0.24	
	evergreen oaks	1.45	0.72	1.00	
	other broadleaves	1.53	0.53	0.24	
	conifers	1.38	0.43	0.29	
	<i>partial total</i>	<i>1.39</i>	<i>0.56</i>	<i>0.27</i>	
	Plantations	eucalyptuses coppices	1.33	0.54	0.43
		other broadleaves coppices	1.45	0.53	0.24
poplars stands		1.24	0.29	0.21	
other broadleaves stands		1.53	0.53	0.24	
conifers stands		1.41	0.43	0.29	
others		1.46	0.48	0.28	
<i>partial total</i>		<i>1.36</i>	<i>0.40</i>	<i>0.25</i>	
Protective		rupicolous forest	1.44	0.52	0.42
		riparian forest	1.39	0.41	0.23
		shrublands	1.49	0.63	0.62
		<i>partial total</i>	<i>1.46</i>	<i>0.56</i>	<i>0.50</i>
Total	-	1.38	0.53	0.30	

**The For-est (Forest Estimates) Model**

In forest science, estimates of the current increment has always been related with age of forest stand (as in yield tables) in order to define the proper rotation period, which depends on age and productivity of the stand. Age could be the best parameter for productivity assessment of single trees, but it is not always appropriate for estimates at the stand level. This is particularly true for natural stands, where forest dynamics is driven by optimised use of natural resources, which includes tree mortality and natural regeneration in gaps. These processes result in a complex mosaic of different ages or cohortes; under these conditions the use of age dependant relationships for productivity estimations is not always appropriate.

The type of forest management outlined

above is especially common in Mediterranean countries, where even-aged stand is



**Fig. 1** - Example of Richards function (first derivative) fitting - *Larix decidua*. Comune di Cesana Torinese (TO) - Piano d'assestamento 1963-1972. Parameters: a = 446.1937; k = 0.0336; v = 0.4889; y<sub>0</sub> = 0.21719; R<sup>2</sup> = 0.9149003; ME = 0.9157618.

not the rule. Correspondingly, Garcia (1993) writes: "The use of age on the right-hand-side (as independent variable) is conceptually unsatisfactory in that, at least in the sense of elapsed time *t*, it does not have a physical presence (other than as a number of growth rings), and therefore should not be given a causal meaning. Actually, when foresters say *age* they often think *size*."

Lähde et al. (1994) made an analysis on the relation between variables for various forest structures and compositions, showing a higher correlation between current increment and growing stock compared to current increment and age.

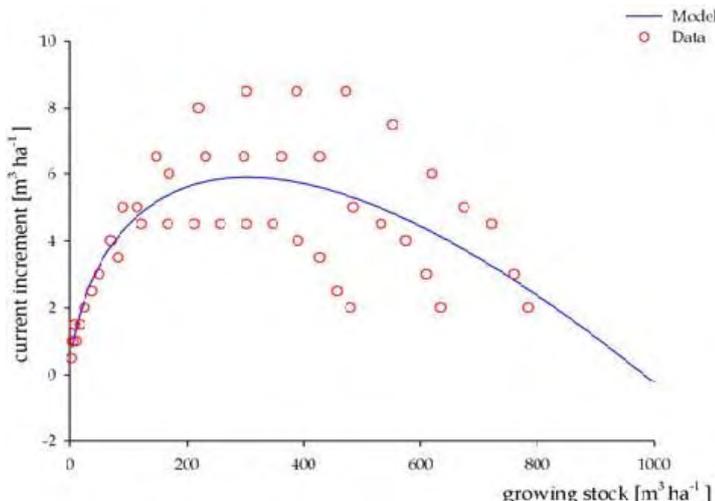
There are various studies showing a relation among dimensional attributes of trees without considering the age (Moser & Hall 1969, Zeide 1993, Thrower 2003, Garcia 1979, Garcia 1983, Rennolls 1995, Birch 1999, Damgaard 1998, Damgaard 1999, Damgaard et al. 2002, Khatouri & Dennis 1990, Atta-Boateng & Moser 2000, Wyszomirski et al. 1999, Duerr & Gevorkiantz 1938, Kolström 1993, Moser 1972). For instance, Chrimes (2004) demonstrates that current increment is directly and significantly related to volume.

Thrower (2003) formulated an equation that calculates current increment as a function of growing stock and of Potential Site Index (PSI) considering this as a variant of the Langsaeter curve, which consists in a univocal relation between stand density and current increment (Langsaeter 1944).

For these reasons, and because of the large majority of Italian forest are not even-aged, we propose to use an approach based on growth curves not dependant on age but considering the growing stock as independent variable and the current increment as dependent one.

We further propose that all carbon stocks in carbon pools shall be estimated in function of the growing stock. This is an advantage compared to other approaches since the growing stock is closely related with other carbon budget components such as soil car-

**Fig. 2** - Example of Richards function (first derivative) fitting - *Picea excelsa*. Comune di Borno (BS). (Parameters:  $a = 978.6552$ ;  $k = 0.0139$ ;  $v = -0.2757$ ;  $y_0 = 0.06267$ ;  $R^2 = 0.54880459$ ;  $ME = -2.794501$ ).



bon, litter, deadwood etc. and it is a unique driver, simply assessable, widely and iteratively sampled on national territory (by NFIs). Moreover, growing stock data could be verified using independent dataset as regional forest inventories and/or local forest management plan.

In order to calculate current increment as a function of growing stock the Richards function (Richards 1959) has been selected. Based on a biologically realistic model, the Richards function is a bounded and a monotonic one, with 4 parameters; it is very appropriate for describing the growth of a particular leaf or of the whole stand (Causton & Venus 1982, Poorter & Van Der Werf 1998) although the presence of 4 parameters makes this function not easy to fit.

The Richards function gives rise to a non-

linear regression situation because the criterion of biological simplicity states that the relative growth of the attributes concerned declines in a mathematically simple manner with increasing size of attribute, but there is sufficient flexibility in the Richards function to allow for varying duration of initial, nearly constant, relative growth rates (*i.e.*, approximation to exponential growth).

The Richards function is defined by the following equation (eqn.1):

$$\frac{dy}{dt} = \frac{k}{v} \cdot y \left[ 1 - \left( \frac{y}{a} \right)^v \right] + y_0 \quad \text{first derivative}$$

The analytical solution of equation 1 is the Richards growth curve (eqn. 2):

$$y = a \cdot \left[ 1 - e^{(\beta - kt)} \right]^{1/v}$$

where general constrain for parameters are:  $a, k > 0$ ;  $-1 \leq v \leq \infty$ ;  $v \neq 0$ .

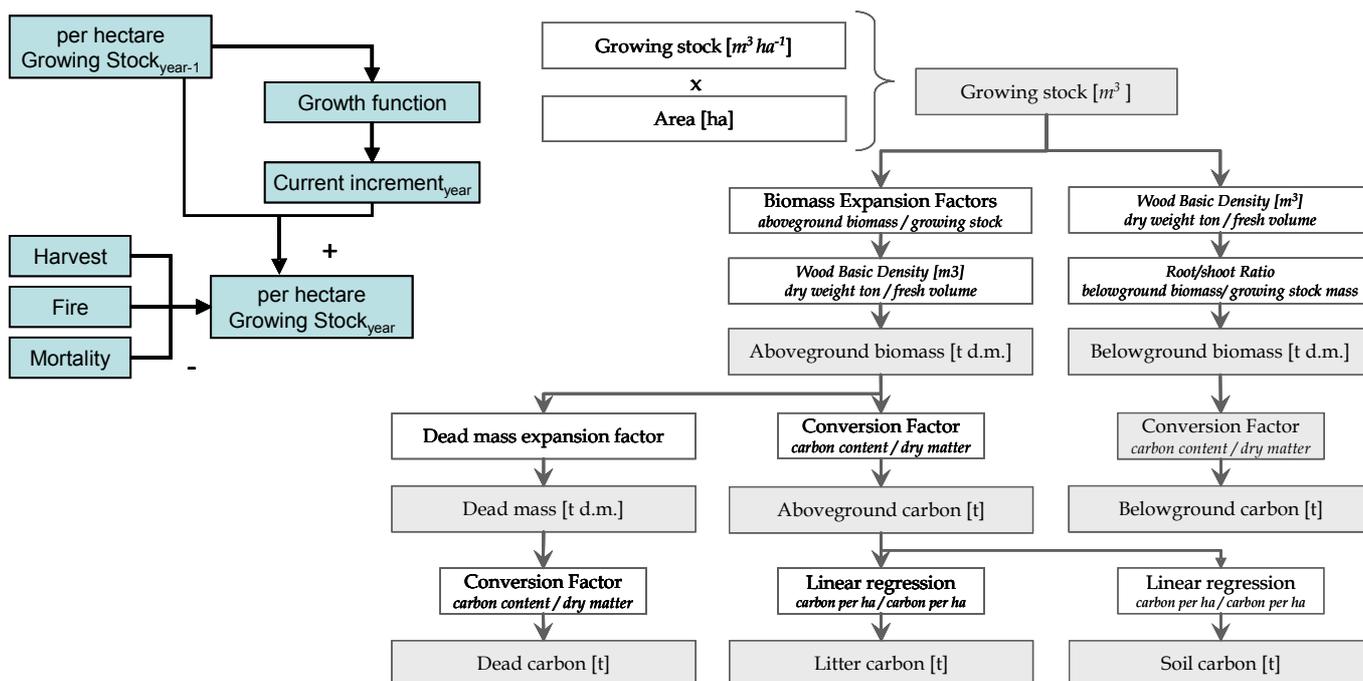
The curve is a generalization of most used growth curves: exponential growth ( $a \rightarrow \infty$ ,  $v > 0$ ), logistic growth ( $v > 1$ ), Bertalanffy function ( $v = 3$ ) and Gompertz function ( $v \rightarrow \pm \infty$ ). This high flexibility is, however, combined with disadvantages as well. The parameters ( $\beta, k, v$ ) have a high covariance which could produce problems during non-linear regression.

Goodness of fit have been evaluated by non-linear coefficient of determination CD (or  $R^2$ ), and performances have been evaluated against data by validation statistics according to Janssen & Heuberger (1995). There, modelling efficiency is defined as:

$$ME = 1 - \frac{\sum_{i=1}^N [Obs_i - Sim_i]^2}{\sum_{i=1}^N [Obs_i - \bar{Obs}_i]^2}$$

where  $Obs_i$  and  $Sim_i$  are, respectively, the observed and the simulated values. In contrast to CD, the modelling efficiency ( $ME$ ) not only measures association (or correlation) between modelled and observed data, but also their coincidence and it is sensitive to systematic deviation between model and observation. When  $ME$  is close to 1 the best performances are obtained.

In the approach followed, the Richards function is fitted through data of growing stock [ $m^3 ha^{-1}$ ] and increment [ $m^3 ha^{-1} y^{-1}$ ] obtained by the collection of Italian yield tables (Federici et al. 2001 - <http://gaia.agraria.unitus.it/download/alsom.html>) because it is the only one data source of forest



**Fig. 3** - Model flowchart.

growing stocks and current increments at national level. The independent variable  $x$  represents growing stock, while the dependent variable  $y$  is the correspondent current increment computed with the Richards function - first derivative.

Such application of Richards function - first derivative - results, generally, in a high coefficient of determination (Fig. 1), that largely decrease with the increase of the number of quality classes forming the yield table (Fig. 2).

### Model structure

Using growing stock as unique driver, the model is able to estimate evolution in time of the five forest carbon pools, classified and defined according to *Good Practice Guidance for LULUCF* (IPCC 2003): aboveground and belowground biomass (living biomass), dead wood and litter (dead organic matter) and soil (soil organic matter - Fig. 3).

The methodology for growing stocks assessment in the years following NFI year is described as following:

1. starting from initial growing stock volume (e.g., growing stock volume reported in the First Italian National Forest Inventory; MAF-ISAF 1988), for each year, the current increment per hectare [ $m^3 ha^{-1} y^{-1}$ ] is computed with the derivative Richards function, for every specific forest typology;
2. for each year, growing stock per hectare

[ $m^3 ha^{-1}$ ] is computed from the previous year growing stock volume adding the calculated current increment ("y" value of the derivative Richards) and subtracting losses due to harvest, mortality and fire occurred in the current year.

The process can be summarized as follows (eqn. 3):

$$gs_i = \frac{gs_{i-1} + I_i - H_i - F_i - M_i (-D_i)}{A_i}$$

in which current increment is calculated year by year by applying the derivative Richards function; and  $gs_i$  is the volume per hectare of growing stock for current year;  $gs_{i-1}$  is the total previous year growing stock volume;  $I_i$  is calculated as  $f(v_{i-1}) \cdot A_{i-1}$  and is the total current increment of growing stock for current year;  $f$  is the Richards function reported above;  $v_{i-1}$  is the previous year growing stock volume per hectare;  $A_{i-1}$  is the total area referred to a specific forest typology for previous year;  $H_i$  is the total amount of harvested growing stock for current year;  $F_i$  is the total amount of burned growing stock for current year;  $M_i$  is the total amount of growing stock removed by natural mortality;  $D_i$  is the total amount of growing stock removed by drain and grazing (only in the category: protective forest).

Carbon amount released by forest fires has been included in the overall assessment of carbon stocks change. Since data on the fraction of growing stock oxidised as con-

sequence of fires were not available, the most conservative hypothesis has been adopted; all growing stock of burned forest areas has been assumed to be completely oxidised and so released. Moreover, since data on forest typologies of burned areas were also not available, the total value of burned forest area coming from national statistics has been subdivided and assigned to forest typologies based on their respective weight on total national forest area. Finally, the amount of burned growing stock has been calculated multiplying average growing stock per hectare of forest typology for the assigned burned area. Assessed value has been subtracted to total growing stock of respective typology, as afore said.

Once estimated growing stock, amounts of aboveground woody tree biomass, belowground biomass and dead mass are consequently assessed.

### Aboveground biomass

For every forest typology, starting from growing stock data, the amount of aboveground woody tree biomass (d.m.) [t] is estimated, for every forest typology, through the relation (eqn. 4):

$$\text{Aboveground woody tree biomass (d.m.)} = GS \cdot BEF \cdot WBD \cdot A$$

where  $GS$  is the volume of growing stock [ $m^3 ha^{-1}$ ];  $BEF$  is the biomass expansion factor, which expands growing stock volume to volume of aboveground woody biomass;  $WBD$  is the wood basic density [t d.m.  $m^{-3}$  f.v.]; and  $A$  is the forest area occupied by a specific typology [ha].

### Belowground biomass

For every forest typology, applying a Biomass Expansion Factor to growing stock data, the belowground biomass is estimated, with the following relation (eqn. 5):

$$\text{Belowground woody tree biomass (d.m.)} = GS \cdot WBD \cdot R \cdot A$$

where  $GS$  is the volume of growing stock [ $m^3 ha^{-1}$ ];  $R$  is the root/shoot ratio, which converts growing stock biomass in belowground biomass;  $WBD$  is the wood basic density [t d.m.  $m^{-3}$  f.v.];  $A$  is the forest area occupied by a specific typology [ha].

### Dead mass

For every forest typology, the deadwood mass was assessed applying a dead mass conversion factor (DCF, in accordance with table 3.2.2 of GPG for LULUCF - IPCC 2003). The dead mass [t] is (eqn. 6):

$$\text{Deadmass (d.m.)} = GS \cdot BEW \cdot WBD \cdot DCF \cdot A$$

Tab. 3 - Relations: litter and soil carbon - aboveground carbon per ha.

Category	Inventory typology	Relation litter Aboveground C / ha	Relation soil Aboveground C / ha	
Stands	norway spruce	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	silver fir	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	larches	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	mountain pines	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	mediterranean pines	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	other conifers	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	european beech	$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
	turkey oak	$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
	other oaks	$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
	other broadleaves	$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
	Coppices	european beech	$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$
		sweet chestnut	$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$
		horbeams	$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$
other oaks		$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$	
turkey oak		$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$	
evergreen oaks		$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$	
other broadleaves		$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$	
conifers		$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
Plantations		eucalyptuses coppices	$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$
		other broadleaves coppices	$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$
	poplars stands	$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
	other broadleaves stands	$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
	conifers stands	$y = 0.0659x + 1.5045$	$y = 0.4041x + 57.874$	
	others	$y = -0.0165x + 7.3285$	$y = 0.7647x + 33.638$	
	Protective	rupicolous forest	$y = -0.0165x + 7.3285$	$y = 0.7647x + 33.638$
riparian forest		$y = -0.0299x + 9.3665$	$y = 0.9843x + 5.0746$	
shrublands		$y = -0.0299x + 9.3665$	$y = 0.3922x + 65.356$	

where  $GS$  is the volume of growing stock [ $m^3 ha^{-1}$ ];  $BEF$  is the Biomass Expansion Factor which expands growing stock volume to volume of aboveground woody biomass;  $WBD$  is the Wood Basic Density [ $t d.m. m^{-3} f.v.$ ];  $DCF$  is the Dead mass Conversion Factor, which converts aboveground woody biomass in dead mass;  $A$  is the forest area occupied by a specific typology.

### Litter

Total litter carbon amount is estimated from the carbon amount of aboveground biomass with linear relations. Linear relations between stand biomass and litter have been reported in many forest studies (Waring & Running 1998).

### Soil

Applying linear relations, total soil carbon amount is estimated from carbon amount in aboveground biomass, following the same rationale as for litter carbon.

The carbon stocks change of living biomass (LB) is calculated according to *Good Practice Guidance for LULUCF* (IPCC 2003), from aboveground (AG) and belowground (BG) biomass (eqn. 7):

$$\Delta C_{LB} = \Delta C_{AG} + \Delta C_{BG}$$

where total amount of carbon has been obtained from biomass (d.m.), multiplying by the GPG default factor for carbon fraction equal to 0.5.

The Dead Organic Matter (DOM) carbon pool is defined, in the GPG, as the sum of dead wood (D) and litter (L - eqn. 8):

$$\Delta C_{DOM} = \Delta C_D + \Delta C_L$$

The total amount of carbon for dead mass

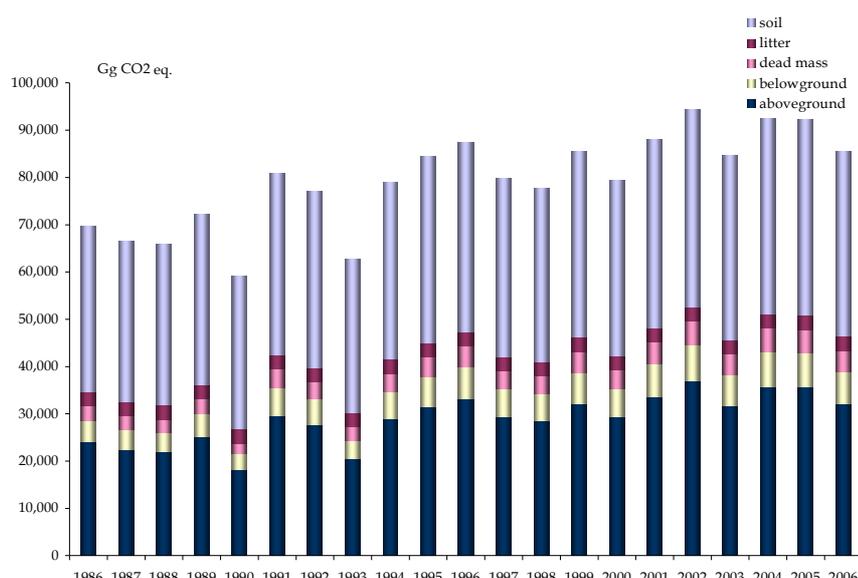


Fig. 5 - Carbon stock changes in the five carbon pools [Gg CO<sub>2</sub> equivalent].

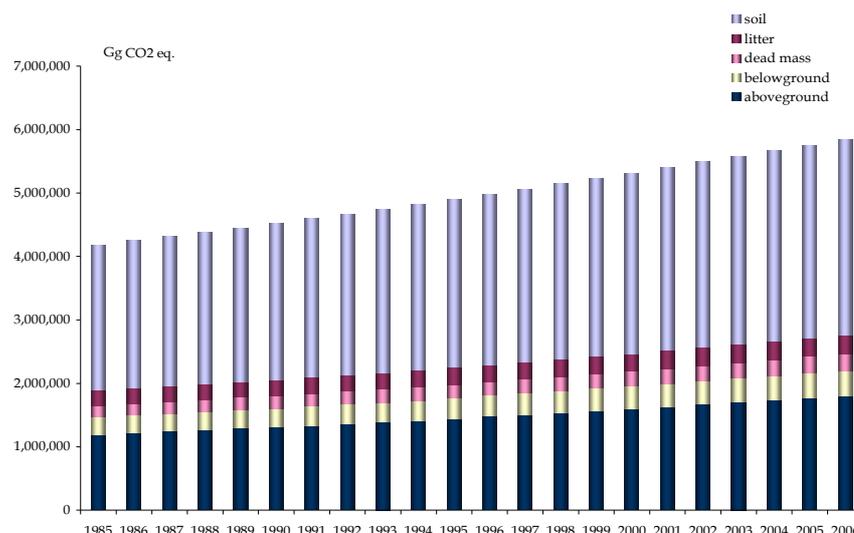


Fig. 4 - Carbon stock in the five carbon pools [Gg CO<sub>2</sub> equivalent].

has been obtained from dead mass (d.m.), multiplying by the GPG default factor for carbon fraction equal to 0.5.

### The Italian dataset

The above-described model has been applied to the Italian dataset, to assess carbon stocks in the five forest pools for reporting year 2007 of the Italian GHG's Inventory.

The model has been applied at regional scale (NUT2) because of availability of any forest-related statistical data. Starting year of the model has been 1985 and estimates have been provided from 1986 to 2006.

Inventory typologies are classified in 4 main categories: Stands, Coppices, Plantations and Protective Forests: (i) *Stands*: norway spruce, silver fir, larches, mountain

pinus, mediterranean pines, other conifers, european beech, turkey oak, other oaks, other broadleaves. (ii) *Coppices*: european beech, sweet chestnut, hornbeams, other oaks, turkey oak, evergreen oaks, other broadleaves, conifers. (iii) *Plantations*: eucalyptuses coppices, other broadleaves coppices, poplar stands, other broadleaves stands, conifers stands, others. (iv) *Protective Forests*: rupicolous forest, riparian forests, shrublands.

Model input data for forest area, detailed by region and by forest typologies, come from the First Italian National Forest Inventory (MAF-ISAFSA 1988) and from the Second Italian National Forest Inventory. Forest area estimation for 1990 has been done through a linear interpolation between the 1985 and 2002 data (pers. comm., MAF-ISAFSA 2004). By assuming that defined trend may well represent near future, it was possible to extrapolate data for 2006.

For each of the five carbon pools, dataset and factors are set as explained in the following sections.

### Woody aboveground biomass

Model input data of growing stocks for the start year (1985), detailed by region and by forest typologies come from the First Italian National Forest Inventory.

The average rate of mortality used for calculation have been 0.0116, concerning evergreen forests, and 0.0117, for deciduous forests, according to GPG for LULUCF (IPCC 2003).

The rate of draining and grazing, applied to protective forest, has been set as 3% following a personal judgement because total absence of referable data.

Total commercial harvested wood, for construction and energy purposes, has been ob-

**Tab. 4** - Carbon stocks in the five carbon pools [Gg CO<sub>2</sub> equivalent].

Year	living biomass		dead organic matter		soil organic matter	total
	aboveground	belowground	dead mass	litter	Soil	
1985	1195445	273629	180432	237858	2296283	4183646
1986	1219454	278155	183507	240877	2331502	4253495
1987	1241906	282299	186357	243926	2365635	4320122
1988	1263786	286372	189130	247061	2399733	4386082
1989	1288949	291217	192312	250061	2435865	4458404
1990	1307136	294627	194425	253141	2468297	4517626
1991	1336836	300486	198270	256090	2506809	4598490
1992	1364584	305907	201852	259086	2544270	4675700
1993	1385098	309730	204595	262246	2576800	4738468
1994	1414023	315450	208465	265223	2614371	4817532
1995	1445453	321838	212575	268160	2653922	4901947
1996	1478567	328579	217010	271103	2694039	4989297
1997	1507848	334508	220890	274093	2731941	5069279
1998	1536363	340190	224707	277042	2768860	5147161
1999	1568504	346799	229142	280018	2808277	5232741
2000	1597791	352703	233178	283057	2845515	5312244
2001	1631400	359586	237801	286044	2885499	5400330
2002	1668344	367203	242900	288986	2927452	5494885
2003	1700073	373692	247282	291995	2966507	5579550
2004	1735805	381056	252229	294992	3008005	5672088
2005	1771367	388414	257127	297971	3049532	5764411
2006	1803549	395100	261601	300992	3088758	5850001

tained from national statistics (ISTAT 2008a); even if data on biomass removed in commercial harvest published by ISTAT are probably underestimated, particularly concerning fuelwood consumption (ARPA Lombardia 2007). Data of wood use for construction and energy purposes, reported in m<sup>3</sup>, are disaggregated at NUT2 level, in sec-

tional statistics (ISTAT 2008a, 2008b, 2008c) or at NUT1 level for coppices and high forests in national statistics. These figures have been subtracted, as losses, to growing stock volume, as mentioned above.

Biomass Expansion Factors for conversions from growing stock volume to volume of aboveground biomass have been derived

for each forest typology, using preliminary results of the *RiservaItalia Project* carried out by ISAFSA (ISAFSA 2004), as follows:

- for broadleaves and pines with large crown: starting from stump, volume of whole woody biomass over bark up to 3 cm of diameter of all trees with diameter at breast height  $\geq 3$  cm;

**Tab. 5** - Carbon stock changes in the five carbon pools [Gg CO<sub>2</sub> equivalent].

Year	living biomass		dead organic matter		soil organic matter	total
	aboveground	belowground	dead mass	litter	soil	
1986	24009	4526	3076	3019	35219	69848
1987	22452	4145	2849	3049	34133	66627
1988	21881	4073	2773	3135	34098	65960
1989	25163	4844	3183	3001	36132	72322
1990	18187	3410	2113	3079	32432	59222
1991	29700	5859	3845	2949	38512	80864
1992	27748	5422	3582	2996	37462	77209
1993	20514	3822	2743	3159	32529	62768
1994	28925	5721	3870	2977	37572	79064
1995	31430	6388	4110	2937	39550	84415
1996	33114	6742	4435	2943	40117	87350
1997	29281	5928	3880	2991	37902	79982
1998	28515	5682	3817	2949	36919	77882
1999	32141	6610	4436	2976	39417	85580
2000	29287	5903	4036	3039	37238	79503
2001	33609	6883	4623	2986	39984	88086
2002	36945	7617	5099	2942	41952	94555
2003	31729	6489	4383	3010	39055	84665
2004	35732	7364	4947	2996	41498	92538
2005	35562	7358	4897	2979	41526	92323
2006	32182	6686	4474	3021	39227	85590

- for conifers: starting from stump, wood volume of stem over bark up to 3 cm of diameter of all trees with diameter at breast height  $\geq 3$  cm.

Wood Basic Densities for conversions from fresh volume to dry weight have been derived for each forest typology, from Giordano 1980. In Tab. 2 BEF's and WBD's are reported.

#### Belowground biomass

Also in this case, the values for root/shoot ratio  $R_s$ , reported in Tab. 2, were derived for each forest typology, in the same way as for aboveground biomass. Values refer to all living biomass of live roots; fine roots of less than (suggested) 2 mm diameter are often excluded because these often cannot be distinguished empirically from soil organic matter or litter.

#### Dead mass

The deadwood mass was assessed applying a dead mass conversion factor (DCF of respectively 0.2 for evergreen forests and 0.14 for deciduous forests, as reported in Tab. 3.2.2 of GPG - IPCC 2003).

#### Litter

It includes all non-living biomass with a diameter less than a minimum diameter chosen by the country for lying dead (for example 10 cm), in various states of decomposition above the mineral or organic soil. This includes the litter, fomic, and humic layers. Live fine roots (of less than the suggested diameter limit for below-ground biomass) are included in litter where they cannot be distinguished from it empirically.

Up to now we do not have a full comprehensive data set to establish a more proper biophysical relation for Italian forests. But collection of data in the Italian new national

**Tab. 6** - NFI's and estimated current increment values for different forest typologies (stands).

Forest typology	current increment reported in the 1 <sup>st</sup> NFI (1985)	current increment estimated with Richards functions
<b>high stands</b>	<b>m<sup>3</sup> ha<sup>-1</sup></b>	<b>m<sup>3</sup> ha<sup>-1</sup></b>
norway spruce	9.4	5.7
silver fir	9.2	7.0
larches	5.7	4.4
mountain pines	8	8.5
mediterranean pines	7.1	8.7
other conifers	13.6	6.5
european beech	8.5	7.0
turkey oak	6.7	5.2
other oaks	4.6	4.3
other broadleaves	8.8	5.2
<i>average</i>	<i>7.9</i>	<i>6.3</i>

forest inventory should allow to analyze the relationship and to choose most appropriate mathematical representation. For present work we have used the results of the European project CANIF ([http://www.bgc-jena.mpg.de/bgc-processes/research/Schulze\\_Euro\\_CANIF.html#contents](http://www.bgc-jena.mpg.de/bgc-processes/research/Schulze_Euro_CANIF.html#contents)) which has reported such relations for a number of European forest stands. The total litter carbon amount has been estimated from above-ground carbon amount with linear relations differentiated per forestry use: stands (resinous, broadleaves, mixed stands) and coppices (Tab. 3).

#### Soil

To this purpose we have used data coming from a number of permanent plots, distributed in several forest typologies, within the project CONECOFOR (<http://www.corpo-forestale.it/wai/serviziattivita/CONECOFOR/index.htm>) of the Italian Ministry of Agri-

culture and Forestry, which provided data on stand biomass and soil carbon. Per forestry use: stands (resinous, broadleaves, mixed stands) and coppices, total soil carbon amount [t C ha<sup>-1</sup>] has been estimated from carbon amount of total woody aboveground biomass [t C ha<sup>-1</sup>], with linear relations. In Tab. 3 the used relations have been reported.

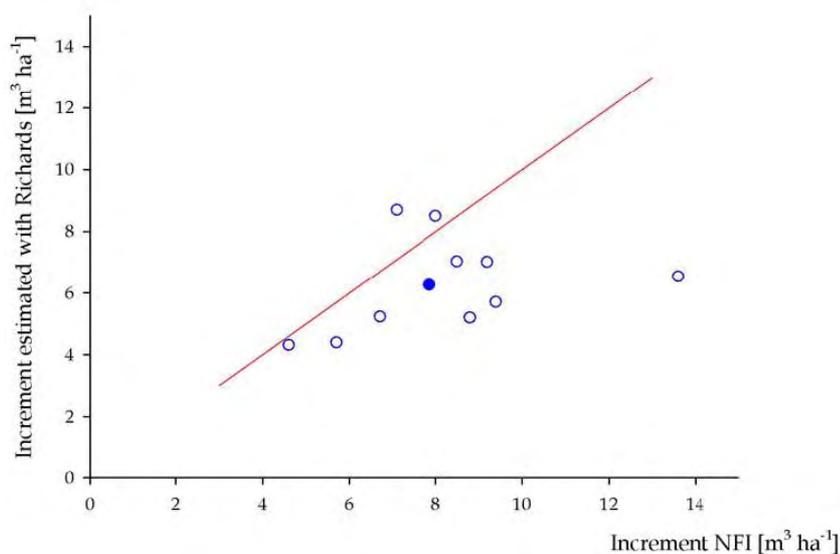
## Results and discussion

In the reported case of study, the Forest model has been applied to Italian dataset, in order to provide estimates of carbon stocks changes in the five forest pools: above-ground, belowground and dead mass, soil and litter (Fig. 4). In the following tables (Tab. 4 and Tab. 5), carbon stocks in the above mentioned pools and carbon stock changes are shown.

It can be noted that in 2006 the Italian total carbon stock in forest sector amounts to about 5.8 Gt CO<sub>2</sub> with the largest pool constituted by soil carbon. The ratio of above-ground biomass to soil carbon is about 0.58 which is higher than the one (circa 45%) calculated for other European countries from the data reported in the FAO - Global Forest Resources Assessment (UN/ECE-FAO 2005). The three other pools (below ground, dead wood and litter) are almost equivalent and amount to about 7%, 4% and 5% of total, respectively.

The increasing trend of the five pools reflects in this case the expansion of forest areas which occurred in the period 1986 - 2006.

By contrast stock changes in aboveground biomass are comparable with changes in soil carbon stocks (Fig. 5). The values showed in Tab. 5, if reported at the stand level shows an average 1986-2006 accumulation rate of 7.94 t CO<sub>2</sub> ha<sup>-1</sup> y<sup>-1</sup> (living biomass 3.47 t CO<sub>2</sub> ha<sup>-1</sup> y<sup>-1</sup>; dead organic matter: 0.69 t CO<sub>2</sub> ha<sup>-1</sup> y<sup>-1</sup>; soil: 3.79 t CO<sub>2</sub> ha<sup>-1</sup> y<sup>-1</sup>). In general, this result seems to show some overestimation of



**Fig. 6** - Current increment reported on NFI vs current increment estimated with Richards.

**Tab. 7** - Relations for assessing uncertainties of C pools.

Carbon pool	Relation for uncertainty assessing
Aboveground	$E_{AB,1985} = (E_{NFI}^2 + E_{BEF}^2 + E_{BD}^2 + E_{CF}^2)^{0.5}$
Belowground	$E_{BG,1985} = (E_{NFI}^2 + E_R^2 + E_{BD}^2 + E_{CF}^2)^{0.5}$
Dead mass	$E_{D,1985} = (E_{AG,1985}^2 + E_{DCF,1985}^2)^{0.5}$
Litter	$E_{L,1985} = (E_{LS,1985}^2 + E_{LR,S}^2)^{0.5}$
Soil	$E_{S,1985} = (E_{SS,1985}^2 + E_{SR,S}^2)^{0.5}$

soil carbon changes, and it is due also to the fact that when new forest area is added then, automatically, the whole soil carbon stock of such area is added to the total resulting in an increase of total carbon stock that is actually no more than a shifting of stocks from one land use category (*i.e.*, grassland) to another (*i.e.*, forest land).

Tab. 6 shows values of current increment reported on National Forest Inventory (MAF 1986) for different forest typologies. In the same table, the values of current increment assessed by Richards functions are also reported, calibrated on yield tables data. Com-

**Tab. 9** - Uncertainties related to carbon pools and overall uncertainty for year 1985.

Aboveground biomass	$E_{AG}$ 42.59%
Belowground biomass	$E_{BG}$ 42.59%
Dead mass	$E_D$ 52.10%
Litter	$E_L$ 161.22%
Soil	$E_S$ 152.05%
Overall uncertainty	$E_{1985}$ 84.91%

**Tab. 10** - Overall uncertainties 1985 - 2006.

Year	Perc.
1985	84.91%
1986	84.81%
1987	88.09%
1988	88.32%
1989	88.26%
1990	88.25%
1991	88.15%
1992	87.97%
1993	87.93%
1994	87.84%
1995	87.65%
1996	87.46%
1997	87.32%
1998	87.22%
1999	87.07%
2000	86.93%
2001	86.77%
2002	86.57%
2003	86.41%
2004	86.27%
2005	86.09%
2006	85.97%

parison between measured and estimated values is only feasible for high stands, since only for this silvicultural system the values of current increments are reported in the first NFI.

In Fig. 6, current increments estimated with the Richards function are plotted against current increment data obtained by the first Italian NFI. Because wide majority of the points are in

the lower half of Cartesian field, it is possible to state that the model shows a systematic underestimation of current increments (in particular the estimated average value is 20% smaller).

The mismatch between the estimated and reported NFI data is likely to be caused by a general disagreement between yield tables and the real average quality of forest sites in the country. The Richards function was parametrised using all yield tables quality classes, on average, without weighting different contributes of different classes.

Moreover, the available yield tables are somewhat outdated since they were compiled mainly during the years 1950-1970. Nowadays a higher current increment than in the past is most likely, as confirmed in other countries like Germany (see <http://www.bundeswaldinventur.de>) due to increased temperatures, atmospheric CO<sub>2</sub> concentration and nitrogen deposition (Magnani et al. 2007), as well as changes in forest management, based also on the conclusion of the IPCC expert meeting on current scientific understanding of the processes affecting terrestrial carbon stocks and human influences upon them (Geneva, Switzerland 21-23 July 2003).

Beside to the possible underestimate of current increment, it should be noted that losses by harvested wood are underestimated too, particularly concerning fuelwood consumption. In the estimation process of growing stock time series, a sort of compensation is very likely to occur between underestimated current increment and underestimated harvesting.

Further improvements in refining current increment estimate will be possible when more basic data and information from the second national forest inventory will be available.

#### Uncertainty

To assess overall uncertainty related to estimates for years 1990-2006, we followed the GPG Tier 1 Approach. The uncertainty linked to the year 1985, when first National Forest Inventory was carried out, was calcu-

$$E_{1985} = \frac{\sqrt{\sum_i (E_{i,1985} \cdot V_{i,1985})^2}}{\sum_i |V_{i,1985}|}$$

**Tab. 8** - Carbon stocks and uncertainties for year 1985 and current increment related uncertainty. (a) The current increment is estimated by the Richards function (first derivative); uncertainty has been assessed considering the standard error of the linear regression between the estimated values and the corresponding current increment values reported in the National Forest Inventory. (b) Good Practice Guidance default value (IPCC 2003).

Carbon stocks t and CO <sub>2</sub> eq. ha <sup>-1</sup>	Aboveground biomass	$V_{AG}$ 137.8
	Belowground biomass	$V_{BG}$ 31.5
	Dead mass	$V_D$ 20.8
	Litter	$V_L$ 27.4
	Soil	$V_S$ 264.7
Uncertainty	Growing stock	$E_{NFI}$ 3.2%
	Current increment (Richards) <sup>(a)</sup>	$E_{NFI}$ 51.6%
	Harvest <sup>(b)</sup>	$E_H$ 30%
	Fire <sup>(b)</sup>	$E_F$ 30%
	Drain and grazing	$E_D$ 30%
	Mortality	$E_M$ 30%
	BEF	$E_{BEF1}$ 30%
	R	$E_{BEF2}$ 30%
	DCF	$E_{DEF}$ 30%
	Litter (stock + regression)	$E_L$ 161%
	Soil (stock + regression)	$E_S$ 152%
	Basic Density	$E_{BD}$ 30%
	C Conversion Factor	$E_{CF}$ 2%

lated with the relation (eqn. 9):

where overall uncertainty  $E$  is expressed by the terms  $V_i$  indicating each of the carbon stocks of the five pools for the year 1985 ( $i = AG$ : aboveground,  $BG$ : belowground,  $D$ : dead mass,  $L$ : litter,  $S$ : soil), while, with letter  $E$ , related uncertainties have been indicated. Tab. 7 shows the equations for assessing the overall uncertainties associated to the carbon pools.

Terminology for aboveground:  $E_{NFI}$  = uncertainty associated to growing stock data given by the first National Forest Inventory;  $E_{BF}$  = uncertainty related to biomass expansion factors for aboveground biomass;  $E_{BD}$  = uncertainty of the basic density;  $E_{CF}$  = uncertainty of the conversion factor, where GPG default values for uncertainty assessment have been used (IPCC 2003).

Terminology for belowground:  $E_R$  = uncertainty of root-shoot-ratio taken from GPG default. Concerning dead mass relation,  $E_{DCF}$  = uncertainty of dead mass expansion factor, taken from GPG default;  $E_{LS,1985}$  and  $E_{SS,1985}$  = uncertainties related to litter and soil carbon stock data taken from CANIF project and CONECOFOR Programme, respectively. Finally, the terms  $E_{LR,1985}$  and  $E_{SR,1985}$  are defined as uncertainties related to linear regressions used to assessing litter and soil carbon stocks. Tab. 8 shows the values of carbon stocks in the five pools for year 1985, with the associated uncertainties.

Tab. 9 shows the uncertainties related to in-

**Tab. 11** - Comparison between modeled and NFI preliminary 2006 aboveground carbon stock.

NFI aboveground carbon stock (tC)	For-est model related to 2006 (tC)
486018500	491877087

dividual carbon pools and the overall uncertainty for 1985, as based on the equations in Tab. 7.

The overall uncertainty related to 1985 (year of the first National Forest Inventory) was propagated until 2006, following the Tier 1 approach.

The equations for the year following to 1985 are similar to the one for the 1985 uncertainty estimate, apart from terms linked to aboveground biomass: the biomass increment was computed by the methodology described in *Model structure* paragraph; in consequence, the related uncertainty, e.g., for 1986, is expressed by the following formula (eqn. 10):

$$\hat{E}_{1985} = \frac{\sqrt{\sum_i (E_i \cdot V_i)^2}}{|V_{NFI} + V_I - V_H - V_F - V_D - V_{MOR}|}$$

$$E_{AG1985} = \sqrt{\hat{E}_{1985}^2 + E_{BEF}^2 + E_{BD}^2 + E_{CF}^2}$$

where  $i = NFI, I, H, F, D, M$ .

Following Tier 1 approach and the above mentioned methodology, the overall uncertainty in the estimates produced by the described model has been quantified; in Tab. 10 the uncertainties of the 1985-2006 period are reported.

The overall uncertainty in the model estimates between 1985 and 2006 was assessed with the following relation (eqn. 11):

$$E_{1985-2006} = \frac{\sqrt{(E_{1985} V_{1985})^2 + (E_{2006} V_{2006})^2}}{|V_{1985} + V_{2006}|}$$

where terms  $V_{1985}$  and  $V_{2006}$  represent growing stocks in [ $m^3 ha^{-1} CO_2 eq$ ],  $E$  the uncertainties in the respective years. The overall uncertainty related to the period 1985-2006 is equal to 60.5%.

However, on May 29<sup>th</sup> 2007, during a national workshop on forest statistics, the preliminary data of the new NFI regarding to the 2006 aboveground carbon stock of the whole Italian forest land area were presented. A comparison between our estimate and the preliminary NFI data results in 1.2% difference (Tab. 11).

## Conclusions

The proposed approach has provided both a reanalysis of the Italian forest sector carbon stock changes in accordance with UNFCCC

requirements and estimates of carbon stock changes for years between national forest inventories.

The use of an age-independent relationship for deriving forest growth increment, from growing stocks has been proven more useful than a classical age-growth relationship.

In particular, the approach allows deriving from the growing stock the other carbon budget components, which are usually difficult to obtain, or for which detailed process based models are still far from being operational. Using a single input like growing stock, which is regularly derived from NFI, is particularly useful: it is directly assessed and can more easily be verified by different methodologies like verification plots or remote sensing techniques.

Based on our novel approach, using NFI data of 1985 and including the new forest areas estimates of 2004 (pers. comm., MAF-ISAFA 2004), we calculate an overall carbon stock change for Italian forest in 2006 in the range 85 Mt CO<sub>2</sub>. This estimate is rather conservative since the approach based on an overall Richard function approximation tends to underestimate the observed increment by NFI.

Improvements of the above mentioned approach could be driven by the web-based "AFOLU-Clearinghouse for Policy-Science-Data" under development by JRC, especially with regard to its European level databases of allometric biomass & carbon factors, yield tables and forest inventories (see <http://afoludata.jrc.it/carboinvent/ciintro.cfm>). The approach described above in combination with such database will improve quality control and quality assurance routines (e.g., verification, cross-checking) for national GHG inventories and will help in gap-filling of the forestry sector in the EC-Inventory.

Finally, it is worth to note that data produced by this methodology have been successfully used by the Italian government for the renegotiation of the Italian cap for the forest management activity under Article 3.4 of the Kyoto Protocol (FCCC/KP/CMP/-2006/10/Add.1 - Decision 8/CMP.2, Forest management under Article 3, paragraph 4, of the Kyoto Protocol: Italy). A fundamental step in the renegotiation process has been the peer review of data and methodologies by the UNFCCC experts, resulting in no major findings.

The Italian cap passes from 0.18 Mt C to 2.78 Mt C, with a strong impact on the economic value associated to the Italian forest, being an incentive in the conservation and sustainable management of the forest areas.

## References

ARPA Lombardia (2007). Stima dei consumi di legna da ardere per riscaldamento ed uso domestico in Italia, Rapporto Finale. ARPA Lombardia,

Milano.

Atta-Boateng J, Moser JW (2000). A compatible growth and yield model for the management of mixed tropical rain forest. *Can. J. For. Res.* 30: 311-323.

Birch CPD (1999). A New Generalized Logistic Sigmoid Growth Equation Compared with the Richards Growth Equation. *Annals of Botany* 83: 713-723.

Chrimes D (2004). Stand development and regeneration dynamics of managed uneven-aged *Picea abies* forests in boreal Sweden. Doctoral dissertation, Dept. of Silviculture, SLU. Acta Universitatis agriculturae Sueciae. *Silvestria* vol. 304. ISSN 1401-6230, ISBN 91-576-6538-9.

Causton DR, Venus JC (1982). *The Biometry of Plant Growth*. Edward Arnold, USA.

Damgaard C (1998). Plant Competition Experiments: Testing Hypotheses and Estimating the Probability of Coexistence. *Ecology* 79 (5): 1760-1767.

Damgaard C (1999). A test of asymmetric competition in plant monocultures using maximum likelihood function of a simple growth model. *Ecological Modelling* 116: 285-292.

Damgaard C, Weiner J, Nagashima H (2002). Modelling individual growth and competition in plant populations: growth curves of *Chenopodium album* at two densities. *Journal of Ecology* 90: 666-671.

Duerr WA, Gevorkiantz SR (1938). Growth prediction and site determination in uneven-aged timber stands. *Journal of Agricultural Research* 56 (2): 81-98.

Federici S, Quarantino R, Papale D, Tulipano S, Valentini R (2001). Sistema informatico delle Tavole Alsimetriche d'Italia, DiSAFRi - Università degli Studi della Tuscia. [online] URL: <http://gaia.agraria.unitus.it>

Garcia O (1979). Modelling stand development with stochastic differential equations. In: *Mensuration for Management Planning of Exotic Forest Plantations*, FRI Symposium (Elliot DA ed). N.Z. Forest Serv., Rotorua, New Zealand.

Garcia O (1983). A stochastic differential equation model for the height growth of forest stands. *Biometrics* 39: 1059-1072.

Garcia O (1993). Stand growth models: Theory and practice. In: *Advancement in Forest Inventory and Forest Management Sciences*. Proceedings of the IUFRO Seoul Conference. Forestry Research Institute of the Republic of Korea, pp. 22-45.

UN/ECE-FAO (2005). *Global Forest Resources Assessment 2005. Main Report Italy - Country Report*, UN/ECE-FAO.

Giordano G (1980). *Tecnologia del legno*. Hoepli, Milano.

IPCC (2000). *Good Practice Guidance and Uncertainty Management in National Greenhouse Gas Inventories*. IPCC National Greenhouse Gas Inventories Programme, Technical Support Unit, Hayama, Kanagawa, Japan.

IPCC (2003). *Good Practice Guidance for Land Use, Land-Use Change and Forestry*. IPCC Technical Support Unit, Kanagawa, Japan.

- ISAFSA (2004). RiselvItalia Project. [online] URL: <http://www.ricercaforestale.it/riselvitalia/index.-htm>.
- ISTAT (2008a). Statistiche forestali. Istituto Nazionale di statistica, Roma.
- ISTAT (2008b). Statistiche dell'agricoltura. Istituto Nazionale di statistica, Roma.
- ISTAT (2008c). Annuario Statistico Italiano. Istituto Nazionale di statistica, Roma.
- Janssen PHM, Heuberger PSC (1995). Calibration of process oriented models. *Ecological Modelling* 83: 55-66.
- Lähde E, Laiho O, Norokorpi Y, Saksa T (1994). Structure and yield of all-sized and even-sized conifer-dominated stands on fertile sites. *Ann. Sci. For.* 51: 97-109.
- Khatouri M, Dennis B (1990). Growth-and-yield model for uneven-aged *Cedrus atlantica* stands in Morocco. *Forest Ecology and Management* 36: 253-266.
- Kolström T (1993). Modelling the development of an uneven-aged stand of *Picea abies*. *Scandinavian Journal of Forest Research* 8: 373-383.
- Langsaeter A (1944). Om tynning i enaldret granog furuskog. Referat: Produktionsundersøkelser von Fichtenwald. *Medd. Det norske Skogforsøksvesen* 8: 131-216.
- MAF-ISAFSA (1988). *Inventario Forestale Nazionale. Sintesi metodologica e risultati*. Ministero dell'Agricoltura e delle foreste. Istituto Sperimentale per l'assestamento forestale e per l'Alpicoltura, Trento.
- Magnani F, Mencuccini M, Borghetti M, Berbigier P, Berninger F, Delzon S, Grelle A, Hari P, Jarvis PG, Kolari P, Kowalski AS, Lankreijer H, Law BE, Lindroth A, Loustau D, Manca G, Moncrieff JB, Rayment M, Tedeschi V, Valentini R, Grace J (2007). The human footprint in the carbon cycle of temperate and boreal forests. *Nature* 447: 848-850.
- Masera OR, Garza-Caligaris JF, Kanninen M, Karjalainen T, Liski J, Nabuurs GJ, Pussinen A, de Jong BHJ, Mohren GMJ (2003). Modeling carbon sequestration in afforestation, agroforestry and forest management projects: the CO2FIX V.2 approach. *Ecological Modelling* 164: 177-199.
- Moser JW (1972). Dynamics of an uneven-aged forest stand. *Forest Science* 18: 184-191.
- Moser JW, Hall OF (1969). Deriving growth and yield functions for uneven-aged forest stands. *Forest Science* 15: 183-188.
- Poorter H, Van Der Werf A (1998). Is inherent variation in RGR determined by LAR at low irradiance and by NAR at high irradiance? A review of herbaceous species. In: *Inherent Variation in Plant Growth; Physiological Mechanisms and Ecological Consequences* (Lambers H, Poorter H, van Vuuren MMI eds). Backhuys Publishers, Leiden, The Netherlands, pp. 309-336.
- Richards FJ (1959). A flexible growth curve for empirical use. *Journal of Experimental Botany* 10: 290-300.
- Rennolls K (1995). Forest height growth modeling. *Forest Ecology and Management* 71: 217-225.
- Thrower JS (2003). *Natural and Managed Stand Yield Tables for the Merritt IFPA Innovative Analysis Project: MTI-402*, Prepared for Nicola-Similkameen Innovative Forestry Society Merritt, British Columbia, Canada.
- Waring RH, Running SW (1998). *Forest ecosystems, analysis at multiple scales*. Academic Press, New York, USA.
- Wyszomirski T, Wyszomirska I, Jarzyna I (1999). Simple mechanism of size distribution dynamics in crowded and uncrowded virtual monocultures. *Ecological Modelling* 115: 253-273.
- Zeide B (1993). Analysis of growth equations. *Forest Science* 39: 591-616.