

Supplementary Material

Appendix 1 - Model description.

Log-normal model

The log-normal model (LNM), first proposed by Preston (1948) is based on the central limit theorem. Because species diversity is affected by simultaneous influences of many biotic and abiotic factors, the random variation of these factors will cause species abundances to be a normally distributed (May 1975). The logarithmic form (LNM) is:

$$S_{(R)} = S_0 e^{-(\alpha^2 R^2)} \quad (1)$$

where $S_{(R)}$ is the number of species in the R th octave to the left and to the right of the symmetrical curve, S_0 is the number of species within modal abundance octave and $1/\alpha$ is the width of the distribution (Kevan & Belaoussoff 1997).

Broken stick model

The broken stick model (BSM) was proposed by MacArthur (1957). The environment is compared with a stick of unit length on which $S-1$ points are thrown at random. The stick is broken at these points and the lengths of the S resulting segments are proportional to the abundances of S species. Under the assumption that all species in the community sharing close taxonomic status and with similar competitive capacity, the expected abundance of the i th rarest species among S species and N individual trees is:

$$N_i = \frac{N}{S} \sum_{k=i}^S \frac{1}{k} \quad (2)$$

where k equals to i . The model assumes that the resource allocation among competitive species follows a one-dimensional gradient (MacArthur 1957).

Zipf model

The Zipf model (ZM) was first introduced by Frontier (1985) who assumed that species occupancy is dependent on the actual environmental and physical conditions and the species present. The cost of occupancy of a pioneer species is rather lower than that of late successional species which have higher

requirements of forest ecosystem structure. This assumption reflects a successional process that late settlers are more difficult to survive than first arrivals. The abundance of the i th species is:

$$N_i = Nqi^\gamma \quad (3)$$

where N is the number of individual trees, q the predicted relative abundance of the species with the highest frequency in the community and γ a constant representing the average probability of species occupancy, suggesting as well a priority effect (Frontier 1985).

Niche preemption model

The niche preemption model (NPM) was proposed by Motomura (1932). When species enter an unsaturated habitat at the same time intervals and occupy a part of the niche, the SADs are more likely to form a NPM, which is particularly common for communities affected by only one or few factors. This model assumes that α percent of the total niches is occupied by the most frequent species, the second one occupies α percent of the remaining niches, i.e., $\alpha(1-\alpha)$; by this analogy, the niche occupied by i th species is $\alpha(1-\alpha)^{i-1}$. The species abundance is ranked by the amount of niches they occupy. The expected abundance for the i th species is:

$$N_i = N\alpha(1-\alpha)^{i-1} \quad (4)$$

where N is the total number of individual trees in the community.

Neutral model

The neutral theory (NM) was introduced by Hubbell (2001). The neutral theory makes the following two assumptions: (1) the total number of individual trees species of a community is constant. In a saturated community, the increase of one species will result, to some extent, in a decrease of another species, and (2) there is no difference in functional and physiological traits between species. Species under the neutral theory have identical natality, mortality, immigration and speciation rates. On the basis of these two assumptions, species abundance shows a zero-sum multinomial distribution. The probability distribution of the species follows the following equations (Etienne 2005):

$$P[D|(\theta, J, m)] = \frac{J!}{\prod_{i=1}^S n_i \prod_{j=1}^J \Phi_j!} \frac{\theta^S}{(\theta)_S} \cdot \sum_{A=S}^J \left[K(D, A) \frac{(\theta)_j}{(\theta)_A} \frac{I^A}{(I)_j} \right] \quad (5)$$

$$I = \frac{m(J-1)}{1-m} \quad (6)$$

$$A = \sum_{i=1}^S a_i \leq J \quad (7)$$

$$K(D, A) = \sum_{\left[a_1, \dots, a_s \mid \sum_{i=1}^s a_i = A \right]} \prod_{i=1}^s \frac{\bar{S}(n_i, a_i) \bar{S}(a_{i,1})}{\bar{S}} \quad (8)$$

where S is the total number of species, n_s is the abundance of s th species and $D = (n_1, n_2, k, n_s)$ is the SADs. θ is an index represents a “fundamental diversity” number the greater the θ , the larger the number of species in a community. j is the total number of individual trees. m the immigration rate per unit area. Φ the number of species with j individual trees. i the number of individual trees which migrated to the local community. A is the number of individual trees of the parent generation and a_i the number of individual trees of the parent generation of the i th species. $K(D, A)$ is a multinomial coefficient. The expected species abundance was estimated by taking the means of 100 simulations of neutral communities using the estimated θ and m predicted by a maximum likelihood estimation method and the total number of observed individual trees j (Walker & Cyr 2007).

Reference

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- Hubbell SP (2001). *The unified neutral theory of biodiversity and biogeography*. Princeton University Press.
- Kevan PG, Belaousoff S (1997). Log-normality of biodiversity and abundance in diagnosis and measuring of ecosystemic health: pesticide stress on pollinators on blueberry heaths. *Journal of Applied Ecology* 34:80-80.
- MacArthur RH (1957). On the relative abundance of bird species. *Proceedings of the National Academy of Sciences of the United States of America* 43: 93-295.
- May RM (1975). Patterns of species abundance and diversity. *Ecology & Evolution of Communities*: 81-120.
- Motomura I (1932). On the statistical treatment of communities. *Zoology Management* 44: 379-383.
- Preston FW (1948). The commonness, and rarity, of species. *Ecology* 29: 254-283
- Walker SC, Cyr H (2007). Testing the standard neutral model of biodiversity in lake communities. *Oikos* 116:143-155.

Appendix 2 - R script.

```
##### Dividing the plot into small sampling scales#####  
# The raw data is organized according to the data format of CTFS  
  
scale.data.matrix= function(data,xsize,ysize,gridsize){#xsize and ysize are the side lengths of the  
plot, gridsize is the side length of sampling unit  
  
rowcol.to.index=function (rowno, colno, gridsize, plotdim = c(xsize, ysize))  
{  
  badrc = (rowno <= 0 | colno <= 0 | rowno > plotdim[2]/gridsize |  
    colno > plotdim[1]/gridsize)  
  rowno = rowno - 1  
  colno = colno - 1  
  maxrow = floor(plotdim[2]/gridsize)  
  index = colno * maxrow + rowno + 1  
  if (length(badrc[badrc > 0]))  
    index[badrc] = NA  
  return(index)  
}  
  
gxgy.to.index=function (gx, gy, gridsize, plotdim = c(xsize, ysize))  
{  
  badgxgy = (gx < 0 | gy < 0 | gx >= plotdim[1] | gy >= plotdim[2] |  
    is.na(gx) | is.na(gy))  
  colno = 1 + floor(gx/gridsize)  
  rowno = 1 + floor(gy/gridsize)  
  if (length(badgxgy[badgxgy > 0]))  
    colno[badgxgy] = rowno[badgxgy] = NA  
  return(rowcol.to.index(rowno, colno, gridsize, plotdim))  
}  
  
no=gxgy.to.index (data$x,data$y,plotdim=c(xsize,ysize),gridsize=gridsize)  
data1=na.omit (cbind (data,no))  
qrat=sort (unique (no))  
n=length (qrat)  
sp=unique (data$sp)  
m=length (sp)  
abu.qrat=matrix (0,n,m)  
colnames (abu.qrat)=sp  
rownames (abu.qrat)=qrat  
nobrance.data=data1  
for (i in 1:n)  
{  
  data2=nobrance.data[nobrance.data$no==qrat[i],]  
  for (j in 1:m)  
  {  
    abu.qrat [i,j]=length (data2[data2$sp==sp[j],]$sp)  
  }  
  total.abu=apply (abu.qrat,2,sum)  
  abu.qrat.t=t (abu.qrat)  
  abu.qrat.t2=data.frame (abu.qrat.t,total.abu)  
  abu.qrat.r=abu.qrat.t2[order (-abu.qrat.t2$total.abu),]  
  abu.qrat.f=t (abu.qrat.r)  
  result=abu.qrat.f[-(n+1),]  
  rownames (result)=qrat  
  return (result)  
}  
  
##### Calculating the observed SAD, taking analysis based on data of  
Jioahe at 10m x 10m scale as an example #####  
data.matrix10=scale.data.matrix (data, 800, 500, 10)  
  
obsSAD.fn=function (data) {  
  abundorder=matrix (NA,nrow=dim (data) [1],ncol = dim (data) [2])  
  for (i in 1:dim (data) [1]) {  
    abundorder [i,]=sort (data [i,],decreasing =TRUE)  
  }  
}
```

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Analysing species abundance distribution patterns across sampling scales in three natural forests in Northeastern China

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```
obsSAD=apply(abundorder,2,mean)
return(obsSAD)
}
obsSAD10=obsSAD.fn(data.matrix10)

#####Calculating the expected SAD by neutral model #####
library(untb)
theta=optimal.theta(obsSAD10)
m=optimal.prob(obsSAD10)

SADdata<-as.count(obsSAD10)

count=600 # 600 times simulations
data.result=matrix(0,count,43)
for(i in 1:count){
  line=untb(SADdata,m)
  len=length(line)
  for(j in 1:len){
    data.result[i,j]=line[[j]]
  }
}
neutalexp10=apply(data.result,2,mean)

#Calculating the expected SAD by other modes
library(vegan)
mod<-radfit(obsSAD10)
a<-fitted(mod)
BSMexp10=a[,1]
NPMexp10=a[,2]
LNMexp10=a[,3]
ZMexp10=a[,4]

#####End of the code#####
```

Tab. S1 - The abundance of each species in Changbaishan.

| Species | Abundance | Species | Abundance |
|-----------------------------------|------------------|-------------------------------|------------------|
| <i>Corylus sieboldiana</i> | 27221 | <i>Viburnum opulus</i> | 520 |
| <i>Acer pseudosieboldianum</i> | 18366 | <i>Maackia amurensis</i> | 399 |
| <i>Acer barbinerve</i> | 16817 | <i>Ulmus davidiana</i> | 304 |
| <i>Acer tschonoskii</i> | 12477 | <i>Malus baccata</i> | 191 |
| <i>Acer tegmentosum</i> | 5470 | <i>Rhamnus davurica</i> | 111 |
| <i>Acer pictum</i> | 4175 | <i>Euonymus verrucosus</i> | 105 |
| <i>Pinus koraiensis</i> | 3047 | <i>Lonicera japonica</i> | 52 |
| <i>Eleutherococcus senticosus</i> | 2594 | <i>Sorbus aucuparia</i> | 51 |
| <i>Tilia amurensis</i> | 2502 | <i>Euonymus phellomanus</i> | 32 |
| <i>Syringa reticulata</i> | 2102 | <i>Sorbaria sorbifolia</i> | 31 |
| <i>Philadelphus schrenkii</i> | 1856 | <i>Populus ussuriensis</i> | 29 |
| <i>Acer ukurunduense</i> | 1845 | <i>Populus koreana</i> | 17 |
| <i>Prunus maximowiczii</i> | 1774 | <i>Phellodendron amurense</i> | 9 |
| <i>Quercus mongolica</i> | 1402 | <i>Betula platyphylla</i> | 8 |
| <i>Acer mandshuricum</i> | 1348 | <i>Sambucus williamsii</i> | 7 |
| <i>Sorbus alnifolia</i> | 942 | <i>Aralia elata</i> | 5 |
| <i>Prunus padus</i> | 924 | <i>Ribes mandshuricum</i> | 5 |
| <i>Ulmus laciniata</i> | 753 | <i>Populus davidiana</i> | 2 |
| <i>Fraxinus mandshurica</i> | 742 | <i>Rosa davurica</i> | 2 |
| <i>Betula costata</i> | 581 | <i>Tilia mandshurica</i> | 2 |
| <i>Euonymus alatus</i> | 525 | <i>Deutzia parviflora</i> | 1 |

Tab. S2 - The abundance of each species in Jiaohe.

| Species | Abundance | Species | Abundance |
|-------------------------------|-----------|-----------------------------------|-----------|
| <i>Carpinus cordata</i> | 6576 | <i>Ulmus davidiana</i> | 62 |
| <i>Acer barbinerve</i> | 6001 | <i>Betula dahurica</i> | 60 |
| <i>Acer mandshuricum</i> | 5494 | <i>Sorbus aucuparia</i> | 58 |
| <i>Corylus sieboldiana</i> | 4525 | <i>Rhamnus ussuriensis</i> | 51 |
| <i>Acer pictum</i> | 3733 | <i>Euonymus alatus</i> | 37 |
| <i>Ulmus laciniata</i> | 2637 | <i>Populus koreana</i> | 36 |
| <i>Syringa reticulata</i> | 2449 | <i>Eleutherococcus senticosus</i> | 26 |
| <i>Tilia amurensis</i> | 1825 | <i>Betula platyphylla</i> | 24 |
| <i>Acer ukurunduense</i> | 1525 | <i>Lonicera japonica</i> | 23 |
| <i>Acer tegmentosum</i> | 1458 | <i>Aralia elata</i> | 20 |
| <i>Pinus koraiensis</i> | 1303 | <i>Philadelphus schrenkii</i> | 16 |
| <i>Sorbus alnifolia</i> | 998 | <i>Rhamnus davurica</i> | 12 |
| <i>Juglans mandshurica</i> | 784 | <i>Fraxinus chinensis</i> | 12 |
| <i>Betula costata</i> | 755 | <i>Populus davidiana</i> | 10 |
| <i>Phellodendron amurense</i> | 743 | <i>Lonicera chrysantha</i> | 9 |
| <i>Abies holophylla</i> | 656 | <i>Malus baccata</i> | 7 |
| <i>Euonymus phellomanus</i> | 629 | <i>Maackia amurensis</i> | 5 |
| <i>Prunus padus</i> | 588 | <i>Rhamnus schneideri</i> | 4 |
| <i>Fraxinus mandshurica</i> | 385 | <i>Deutzia parviflora</i> | 3 |
| <i>Euonymus verrucosus</i> | 320 | <i>Abies nephrolepis</i> | 3 |
| <i>Prunus maximowiczii</i> | 223 | <i>Sambucus williamsii</i> | 2 |
| <i>Ulmus macrocarpa</i> | 186 | <i>Salix koreensis</i> | 2 |
| <i>Quercus mongolica</i> | 151 | <i>Lonicera ruprechtiana</i> | 2 |
| <i>Tilia mandshurica</i> | 99 | <i>Acer triflorum</i> | 1 |

Tab. S3 - The abundance of each species in Liangshui.

| Species | Abundance | Species | Abundance |
|-----------------------------|------------------|-----------------------------------|------------------|
| <i>Abies nephrolepis</i> | 5393 | <i>Prunus padus</i> | 81 |
| <i>Tilia amurensis</i> | 4233 | <i>Picea jezoensis</i> | 63 |
| <i>Acer pictum</i> | 3812 | <i>Rhamnus davurica</i> | 50 |
| <i>Pinus koraiensis</i> | 2606 | <i>Quercus mongolica</i> | 37 |
| <i>Acer tegmentosum</i> | 2039 | <i>Corylus sieboldiana</i> | 33 |
| <i>Acer ukurunduense</i> | 2012 | <i>Phellodendron amurense</i> | 14 |
| <i>Betula costata</i> | 1694 | <i>Populus cathayana</i> | 9 |
| <i>Alnus hirsuta</i> | 1477 | <i>Populus ussuriensis</i> | 8 |
| <i>Fraxinus mandshurica</i> | 1112 | <i>Eleutherococcus senticosus</i> | 7 |
| <i>Betula platyphylla</i> | 709 | <i>Salix matsudana</i> | 5 |
| <i>Picea asperata</i> | 707 | <i>Abies holophylla</i> | 4 |
| <i>Picea koraiensis</i> | 577 | <i>Lonicera japonica</i> | 3 |
| <i>Syringa reticulata</i> | 494 | <i>Populus nigra</i> | 3 |
| <i>Ulmus davidiana</i> | 318 | <i>Rhamnus diamantiaca</i> | 3 |
| <i>Populus davidiana</i> | 275 | <i>Maackia amurensis</i> | 2 |
| <i>Amygdalus davidiana</i> | 146 | <i>Juglans mandshurica</i> | 1 |